

Problems for Capacitors and Inductors

After LC1a Introduction (Capacitors)

1. Determine the charge stored on a $2.2 \mu\text{F}$ capacitor if the capacitor's voltage is 5 V .
Answer: $11 \mu\text{C}$,
2. In some integrated circuits, the insulator or dielectric is silicon dioxide, which has a relative permittivity of 4. If a square capacitor measuring $10 \mu\text{m}$ on edge, has a capacitance of 100 fF , what is the separation distance between the capacitor's plates, in μm ?
Answer: 35.4 nm .

After LC1c Example (Capacitors)

1. If the voltage across a 47 mF capacitor is found to be $+10 \text{ V}$ at an instant in time, what is the current flowing into the capacitor's positive terminal?
 - a. 470 mA *Wrong - the current depends on the derivative of the voltage.*
 - b. 0 A *Wrong - the current depends on the derivative of the voltage.*
 - c. 213 A *Wrong - the current depends on the derivative of the voltage.*
 - d. insufficient information *Right - the current depends on the derivative of the voltage.*
2. If a constant current of $440 \mu\text{A}$ charges a capacitor of value 2.2 mF , with an initial voltage of 1.25 V , what is the capacitor's final voltage after 10 seconds?
Answer: 3.25 V

After LC1d Power (Capacitor)

1. When the charge on a capacitor is doubled, the stored energy;
 - a. decreases by a factor of 4 *Answer: Wrong*
 - b. decreases by a factor of 2 *Answer: Wrong*
 - c. stays the same *Answer: Wrong*
 - d. increases by a factor of 2 *Answer: Wrong*
 - e. increases by a factor of 4 *Answer: Correct*

2. If the voltage on a 15 mF capacitor changes from 3 V to 4 V, how much additional energy is stored on the capacitor?

Answer: 52.5 mJ

After LC2a Introduction (Inductors)

1. If the current through a 5 mH inductor is increasing at 3 A/s, what is the voltage across the inductor? Answer: 15 mV
2. The current in an 8 μ H inductor is given by $i(t) = 3t + 2$ A. What is the value of the inductors voltage at $t = 2$ s? Answer: 24 μ V

After LC2b Symbol I-V (Inductors)

1. If the voltage across a 10 mH inductor is found to be zero;
- What is the current?
 - 10 mA Wrong: insufficient information.
 - 0 mA Wrong: insufficient information.
 - 10 mA Wrong: insufficient information.
 - none of the above Wrong: insufficient information.
 - unknown Correct: We only know the rate of change of the current is zero.
 - What is the magnitude of the rate of change of the current?
Answer: 1 mA/s
2. The current through a 5 μ H inductor is $3\sin(12,000t)$ mA, What is the voltage across the inductor? Answer: 180 μ V

After LC2d Example (inductor)

1. If the voltage across an inductor is zero, it contains stored energy.
 - True Wrong - the energy stored in an inductor is determined by the current.
 - Unknown Correct - the current determines the stored energy
 - False Wrong - until we know the current, logically, we cannot make this claim.
2. If the current flowing through a 6 H inductor is given by $i(t) = 4\cos(2\pi 60t)$ A, How much energy is stored in the inductor at time $t = 5$ s.? Answer 48 J

After LC3d Inductors in Parallel

1. If $L = 420 \mu\text{H}$, determine the equivalent inductance of each network shown below.

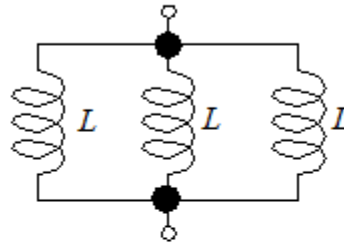
Answers:

a) 1.26 mH

b) 140 μH

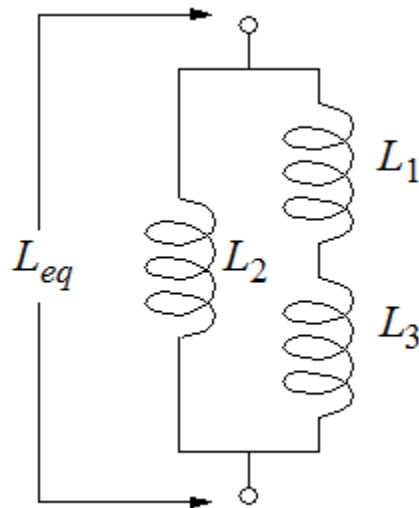


a)



b)

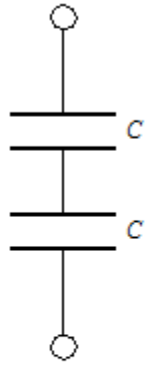
2. If $L_1 = 8 \text{ H}$, $L_2 = 5 \text{ H}$ and $L_3 = 12 \text{ H}$, determine the equivalent capacitance of the network shown to the right. Answer: 4 H



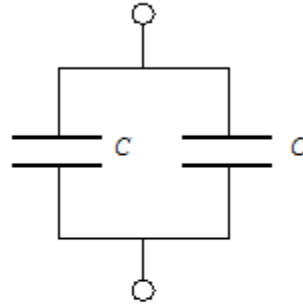
After LC3e Capacitors in Parallel

1. If $C = 90 \text{ F}$, find the equivalent capacitance of each network shown below:

a) $C_{eq} = 45 \text{ F}$, b) $C_{eq} = 180 \text{ F}$



a)



b)

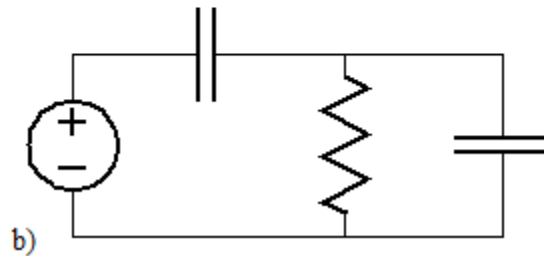
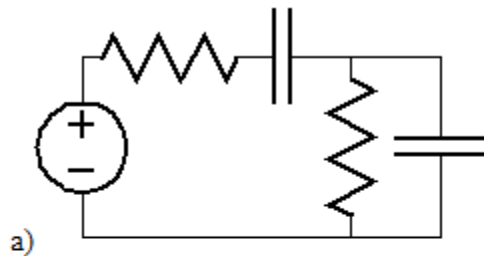
Problems for First Order RC and RL Circuits

After Step 1a Introduction

1. Identify which of the following circuits are first order RC circuits.

a. Yes No Answer: No

b. Yes No Answer: Yes

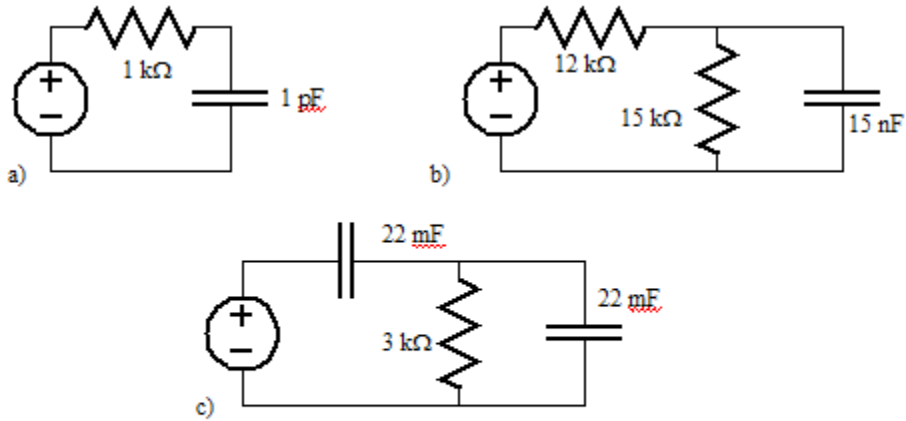


After Step 1b Time Constant

1. Find the time constant for the following circuits;

Answers: a) 1 ns, b) 100 μ s, c) 132 s.

Linear Circuit Problems

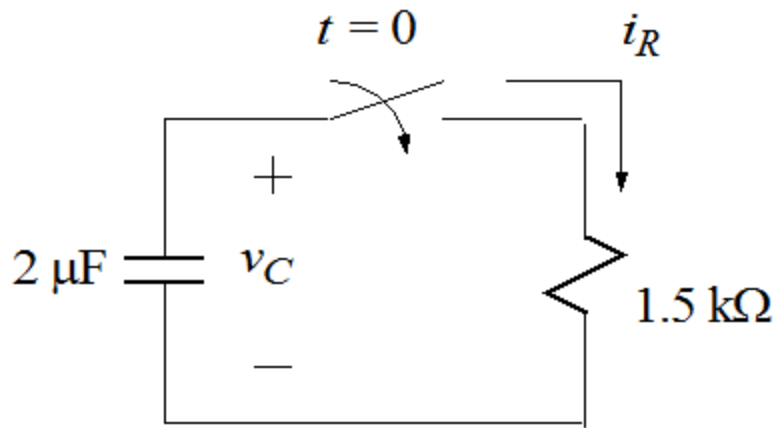


2. If $x(t) = 16e^{-t/10\text{ ns}}$, at what time is the value of x half its value at $t = 0$?
Answer: 6.9 ns.

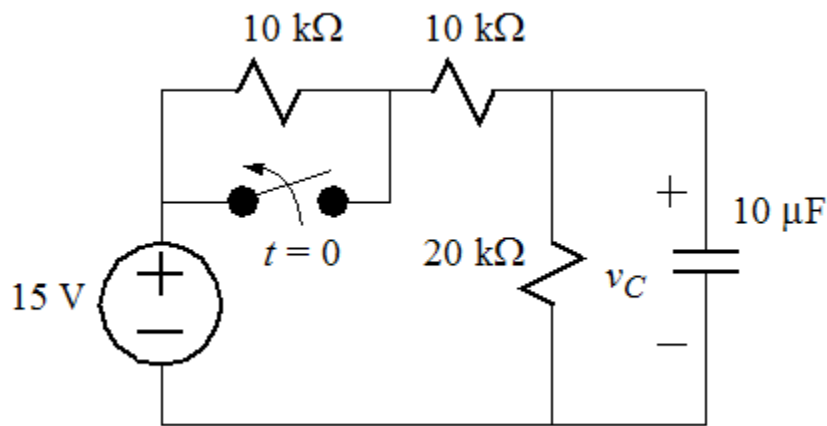
3. If $v(t) = 5 - 5e^{-t/2\text{ ms}}\text{V}$;
 - a. What is the value of v when t is infinite? **Answer: 5 V**
 - b. At what time is the value of v equal to half of its final value? **Answer: 1.4 ms.**

After Step1c Example

1. The capacitor shown below is initially charged to 12 V. If the switch closes at $t = 0$, determine;
 - a. the initial value of the current i_R , after the switch closes. **Answer: 8 mA**
 - b. the time constant for the current after the switch closes. **Answer: 3 ms**
 - c. the value of the current at 4 ms. **Answer: 2.1 mA**
 - d. the time when the current has decreased to 5% of its initial value. **Answer: 9 ms**

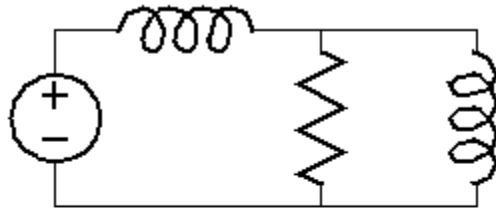


2. If the switch in the circuit shown to the right has been closed a long time and opens at $t = 0$, determine;
- the initial capacitor voltage. **Answer: 10 V.**
 - the capacitor voltage after the switch has been open a very long time. **Answer: 7.5 V**
 - the capacitor voltage after 0.2 s. **Answer: 7.84 V.**

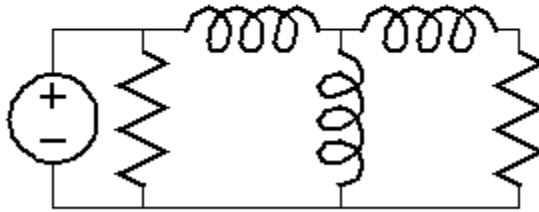


After Step3a RL Natural

1. Identify which of the following circuits are first order RL circuits.
- Yes No **Answer: Yes**
 - Yes No **Answer: No**

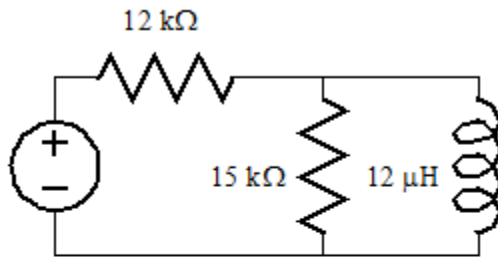


a)

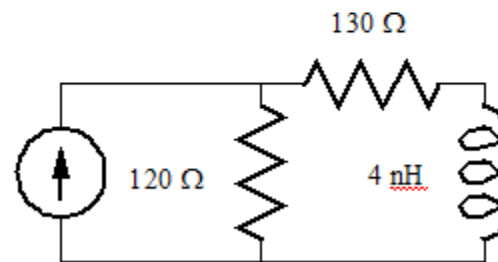


b)

2. Find the time constant for the following circuits;
 Answers a) 1.8 ns, b) 16 ps.



a)

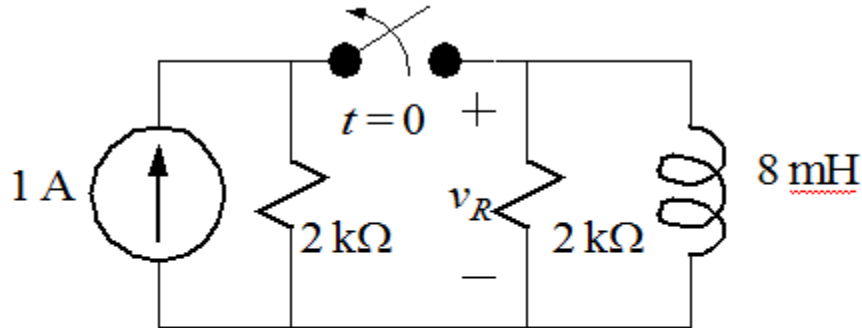


b)

After Step3c RL Step2

1. If the switch in the circuit shown below has been open a long time and closes at $t = 0$, determine;

- a. the initial value of the voltage v_R , after the switch closes. **Answer: 1 V.**
- b. the time constant or the current after the switch closes. **Answer: $2 \mu\text{s}$.**
- c. the value of the voltage at $5 \mu\text{s}$. **Answer: 82 mV.**



After Step3e RL Example

1. The switch in the circuit shown to the right has been open a long time. If the switch closes at $t = 0$ and then re-opens at $t = 50 \text{ ms}$, determine;
 - a. the capacitor's voltage, v_C at $t = 50 \text{ ms}$. **Answer: 6.1 V.**
 - b. the capacitor's voltage at $t = 100 \text{ ms}$. **Answer: 2.7 V.**

